

A Method to Improve Accuracy of Learner Model based on Knowledge and Belief of Learner

Ahmad A. Kardan
Department of Computer Engineering and
Information Technology
AmirKabir University of Technology
Tehran, IRAN
aakardan@aut.ac.ir

Seyede Fatemeh Noorani
Department of Computer
Engineering and Information Technology
Payam-e-Noor University
Tehran, IRAN
f_noorani@pnu.ac.ir

Somayeh Modaberi
Department of Computer Engineering and
Information Technology
AmirKabir University of Technology
Tehran, IRAN
modaberi@aut.ac.ir

Received: January 22 , 2013-Accepted: November 17, 2014

Abstract— The learner model represents essential information about characteristics of learner. The Adaptive Educational Systems and Intelligent Tutoring Systems use learner model to adapt required learning services according to characteristics of each learner. Hence, the accuracy of learner model is an important issue. A learner model is called “open” if its parameters could be inspected, discussed or changed by users. In this paper a novel method is proposed to improve accuracy of learner model based on learner knowledge and learner belief about his/her model. For this purpose the overlay learner modeling with Bayesian networks is used to represent learner knowledge. Then according to nature of open learner model, the learner model is presented as skill meter and learner could state his/her belief about it. Then the model is updated through proposed method. Finally the method is evaluated by use of a comprehensive test and t-student test. The results show our method improves accuracy of learner model.

Keywords: Learner Model, Accuracy of Learner Model, Open Learner Model formatting.

I. INTRODUCTION

Adaptive Educational Systems (AES) and Intelligent Tutoring Systems (ITS) are interesting research domains in e-learning. Utilization of learner model in these systems is the most important characteristic which makes them different from other types of learning environments. In fact, learner model provides necessary information which capable the learning system to adapt its services to learning needs

according to his/her knowledge, background, or other characteristics during the learning process [1, 2].

Open learner models are learner models that can be viewed or accessed in some way by the learner, or by other users (e.g. teachers, peers, parents) [3, 4].

According to the role of learner model in adaptation, the accuracy of learner model is an important issue. In open learner modeling, learner's belief about his/her model could be used as a reference to update learner model [5, 6, 7]. Updating

the learner model in this way doesn't always increase the accuracy of the learner model. In Open Learner personal learner models appropriately; this shows why there should be a mechanism to increase the accuracy in Open Learner Modeling.

In this paper a novel method is proposed to improve the accuracy of learner model based on knowledge and belief in Open Learner Modeling. For this purpose, first the learner knowledge is modeled with overlay learner modeling based on Bayesian networks. Then the model is presented as skill meter and learner could state his/her belief about it. Afterwards the model is updated through proposed method to increase its accuracy. At last the method is evaluated by comprehensive test and t-student test. The results show our method improves the accuracy of learner model.

This paper is structured in four sections. Present section which is an introduction on the work. The background theories are explained in the second section. In section three research methodology and results analysis are described. Finally, section four expresses conclusions and new trends of this work.

II. BACKGROUND THEORIES

A. Learner modeling

As explained in [8] the user modeling is traced back to the works of Allen, Cohen and Perrault (1978, 1979) and Elaine Rich (1989). Learner modeling is the term being selected in e-learning domain.

In [1] Brusilovsky mentioned that a Learner model includes parameters like: knowledge, interests, goals, are necessary: **domain knowledge model** and **overlay knowledge model**.

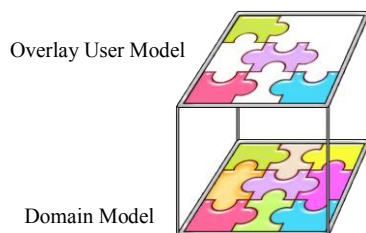


Fig. 1. Overlay knowledge modeling

Domain knowledge model: In this part the general knowledge of domain is divided into a set of domain knowledge fragments which are named as concepts. These concepts are connected to each other, thus some inter-concept inferring is possible. The connection between concepts could be in two forms:

a. A tree of educational objectives, where general objectives are progressively decomposed into specific objectives

b. Concepts can be connected by different kinds of relationships such as: *is-a, has, cause-effect*.

Overlay knowledge model: Overlay knowledge model is way of assigning value to each fragment of domain knowledge. Bayesian network is a common

Modeling learners may not have adequate knowledge to comment about their own educational backgrounds, emotional behaviors, and learning style.

The most important parameter of learner model is knowledge. The learner's knowledge is a dynamic parameter that changes from one session to another session, or even during the same session. Learner's knowledge will increase if the learner learns a new concept, but it may be considered a decline in knowledge if the learner forgets something. A simple and explicit way to obtain the learner's knowledge is taking a quiz. The rate of the correct answers to the quiz is considered as the level of the learner's knowledge in a specific domain.

Modeling techniques such as: scalar [9], overlay [1, 9], perturbation [10] and stereotype [11] can be utilized to model the learner's knowledge.

B. Overlay Modeling

Overlay modeling approach is a dominant approach for learner modeling in ITS and AES. Overlay approach matches properly to the core function of AHS, and provides personalized access to information. Therefore, it has been accepted as de-facto standard by almost all educational and many non-educational adaptive hypermedia systems [1]. So in this work overlay knowledge modeling has been used. The idea of overlay knowledge modeling is to represent the knowledge of each individual user as a subset of a domain knowledge model [12] as illustrated in Fig.1 To model the overlay knowledge two

uncertainty management approach which is used for this purpose.

Overlay knowledge model with Bayesian Networks: The Bayesian Network is a popular representation for encoding uncertain expert knowledge [13]. A Bayesian network is an acyclic directed acyclic graph (**DAG**) where each node **E** represents a domain variable and each arc **V** between nodes represents a probabilistic dependency, quantified using a conditional probability distribution.

General case of Bayesian networks consists of a set of **n** nodes $X = \{X_1, X_2, \dots, X_n\}$ organized in a **DAG**, where each node X_i has parents $pa(X_i)$, the joint probability distribution is compactly expressed as

$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i | pa(x_i)) \quad (1)$$

Bayesian networks most often represent causal statements of the kind $X \rightarrow Y$, where **X** is a cause of effect **Y**. Reverend Thomas Bayes (1702–1761) provided the famous **Bayes' rule**:

$$P(X | Y) = \frac{P(Y | X)P(X)}{P(Y)} = \frac{P(X, Y)}{P(Y)} \quad (2)$$

Note also:

$$P(Y) = \sum_x P(Y | X)P(X) = \sum_x P(X, Y) \quad (3)$$

Bayesian Networks provide two important capabilities: diagnosis (inferences about possible



causes of an event) and prediction (future state/evolution of variables given evidence). Learner modeling is a domain in which there are many different sources of uncertainty and/or imprecision, therefore numerically approximate reasoning techniques like Bayesian networks is suitable for this purpose [14, 15, 16].

In a learner model based on Bayesian Network, internal nodes represent the concepts of the knowledge domain model and the leaf nodes represent the evidences. The sources of evidence are the results of learner interaction with the system (e.g. answers to questions or exercises, time spent reading certain content, number of clicks, etc.).

C. Open Learner Modeling

An Open Learner Model makes a machine’s representation of the learner available as an important means of support for learning. This means that a suitable interface is created for use by learners, and in some cases for others who aid their learning, including peers, parents and teachers [3].

Opening the learner model generally involves more than simply showing the learner the representations from the underlying system’s model of their knowledge (or other attributes modelled), as these representations are not usually designed for interpretation by humans. Generally the presentation could be made in a graphical or textual way. The purpose of OLM is not dependent on a graphical or textual representation. In fact, the important matter is the comprehensibility and clarity of OLM presentation. The open learner model can be commonly represented in two main categories: simple and complicated [17]. In this paper the skill meter is used, which is the most common way of OLM presentation. As [18] considered, skill meter is a part-shaded bar showing learner progress as a subset of expert knowledge, or the probability that a learner knows a concept.

D. Related Works

One of the main purposes of Open Learner Modeling is improving accuracy of learner model. To accomplish this aim learner model can change according to the idea of learner about his/her learner model. Related works, which focused on this aim, are Mr. Collin [5], STyLE-OLM [6], and ChatBot [7].

In these systems first, learner model is presented to learner then learner can inspect his/her model and negotiate with system. To update learner model according to learner’s belief, two separate belief or confidence measures are considered:

- The first one reflects the learner’s own belief about his/her performance.
- The second one is the system’s evaluation of the learner’s performance. For updating the learner model the equation (4) is used.

$$U = |L-S| \quad (4)$$

In equation (4) Update Measure value is shown by U, L stands for learner confidence and S stands for system confidence, also Update Measure is computed

with the measure of difference between the system confidence and the learner confidence. Learner and system confidence values are expressed in four levels: 1- very sure, 2- almost sure, 3- unsure and 4- completely unsure. If Update Measure is less than or equal to one, the system trusts in learner’s belief. But if trust value is more than one, the system negotiates with the learner for some correction or modification in learner model. For example in such a situation the system supplies another exam and the learner is requested to answer the questions. If the learner correctly answers to the questions, the system will trust to his/her feedback in the process of interaction. Otherwise the system does not trust to learner’s response and learner model is remained unchanged. For instance in table (1) three learner confidence, system confidence and Update Measure for learners a, b and c is shown, also according to Update Measure is determined which user is trustworthy and which one isn’t. Update Measure of a is 1 and b is 0 as Update Measure of both a and b is less equal to 1 they are trustworthy and the model update according to their belief. Update Measure of c is more than 1 so c is not trustworthy so the model won’t updated.

Table 1: Examples of trust value

Learner Name	learner confidence (L)	system confidence (S)	Update Measure (U)	Should Update? (Yes/No)
a	3	4	1	Yes
b	1	3	2	No
c	2	2	0	Yes

III. METHODOLOGY

As mentioned, accuracy of learner model is an important issue. One approach which is used to improve learner model accuracy is open learner modeling. In this paper a novel method is proposed to improve accuracy of learner model based on learner knowledge and learner belief. For this purpose a research plan is arranged (Fig.2). This plan has five steps including: 1) selecting participants and learning concepts, 2) learner modeling, 3) open learner modeling, 4) updating learner model with proposed method, and 5) analyzing the results. Each step will be explained in following subsections.

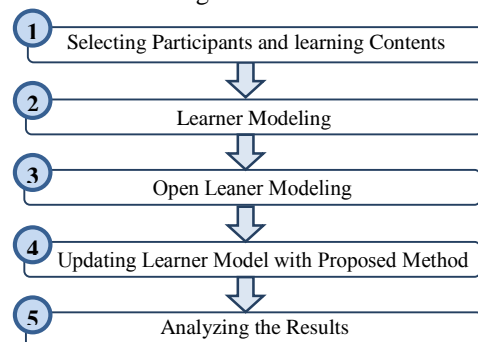
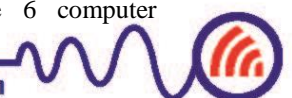


Fig. 2. The paper research plan

A. SELECTING PARTICIPANTS AND LEARNING CONTENTS

Participants characteristic: In this survey, 16 students of Payame Noor University with an average age of 20 participated. They were 6 computer



engineering students, 7 Information Technology students, and 3 math students.

Learning Contents: A part of the Data Structure and Algorithms lesson were selected. The selected contents include:

- C1= “Add and Delete Node in Link List”
- C2=”Scan and Use of Link List”
- C3= “Time Order”
- C4=”Push and Pop and Use of Stack”

As mentioned, in this paper an overlay knowledge modeling approach with Bayesian Network is used. Fig.3a shows knowledge model of learner in which internal nodes represent the concepts of domain and the leaf nodes represent the questions (q1, q2, ..., q12). Each question is about a learning content. For example, as shown in fig 3.a, q1, q2, and q3 are related to concept C1.

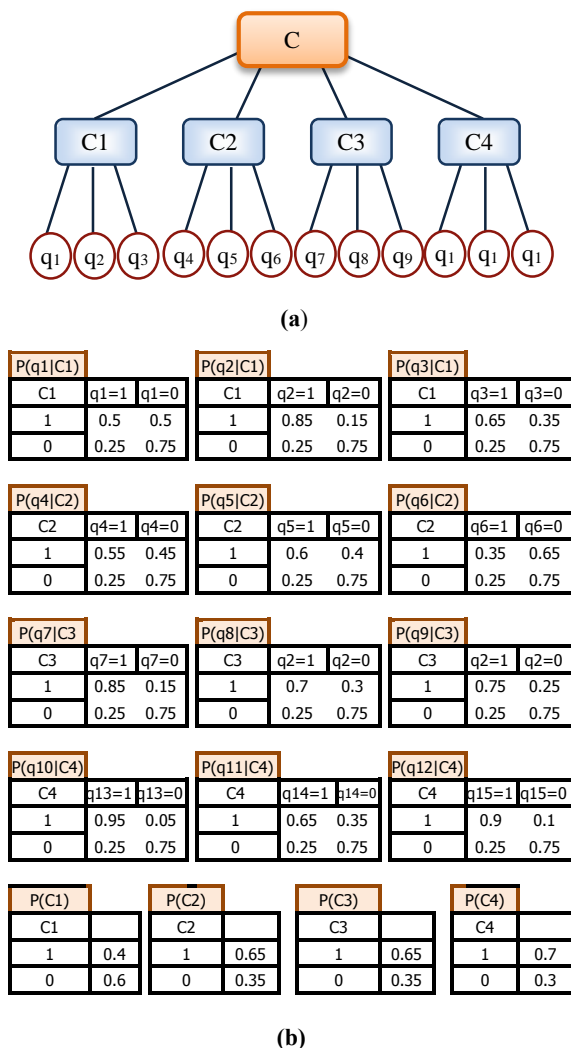


Fig.3. a)The Concepts in Bayesian Network
b) The Conditional Probability Distributions

The possible states of C1... C4 are {1, 0}, that 1 means understanding and 0 means misunderstanding of content Ci. For questions, qi=1(i ∈ {1,...,15}) indicates that learner’s answer is correct and 0 shows the answer is wrong.

Fig.3b shows the conditional probability distributions of each node that were defined by an expert. For example, if the C1 has been understood, we expect the q1 is answered correctly with probability 0.5.

The value of each node is calculated by Bayes’ rule. We use Ki as the value of learner knowledge in each Ci (i ∈ {1,...,4}). In open learner modeling, learner can only observe the value of concepts k1, k2, k3, and k4.

B. LEARNER MODELING

To model the learners’ knowledge, an online multiple choice exam was implemented. The exam consists of 15 questions. Each learner could observe questions. To control the exam condition, for each question the time limit was considered, and the response time was recorded. After exam, using the Bayesian network and exam result, the learners’ knowledge in different concepts was calculated. For example, suppose a given learner’s answers:

- q1=1, q2=1, q3=1, q4=0,
- q5=1, q6=0, q7=1, q8=0,
- q9=1, q10=1, q11=1, q12=0

The knowledge of learner regarding his answers is calculated as follows:

$$\begin{aligned}
 k_1 &= P(C1=1|q1=1, q2=1, q3=1) \\
 &= \frac{P(q1=1, q2=1, q3=1, C1=1)}{P(q1=1, q2=1, q3=1, C1=1) + P(q1=1, q2=1, q3=1, C1=0)} \\
 &= \frac{P(q1=1|C1=1)P(C1=1)P(q2=1|C1=1)P(q3=1|C1=1)P(C1=1)}{P(q1=1|C1=1)P(C1=1)P(q2=1|C1=1)P(q3=1|C1=1)P(C1=1) + P(q1=1|C1=0)P(C1=0)P(q2=1|C1=0)P(q3=1|C1=0)P(C1=0)} \\
 &= \frac{0.5 \times 0.425 \times 0.85 \times 0.65 \times 0.4}{0.5 \times 0.425 \times 0.85 \times 0.65 \times 0.4 + 0.25 \times 0.25 \times 0.25 \times 0.3 \times 0.3} \\
 &= 0.117
 \end{aligned}$$

And:

$$\begin{aligned}
 k_1 &= \frac{P(q1=1|C1=1) \times P(q2=1|C1=1) \times P(q3=1|C1=1) \times P(C1=1)}{P(q1=1|C1=1) \times P(q2=1|C1=1) \times P(q3=1|C1=1) \times P(C1=1) + P(q1=1|C1=0) \times P(q2=1|C1=0) \times P(q3=1|C1=0) \times P(C1=0)} \\
 &= 0.12
 \end{aligned}$$

So:

$$\begin{aligned}
 k_1 &= \frac{P(q1=1|C1=1)P(C1=1)P(q2=1|C1=1)P(q3=1|C1=1)}{P(q1=1|C1=1)P(C1=1)P(q2=1|C1=1)P(q3=1|C1=1) + P(q1=1|C1=0)P(C1=0)P(q2=1|C1=0)P(q3=1|C1=0)} \\
 &= 0.117/0.12 = 0.975
 \end{aligned}$$

The same calculations are used for C2, C3, and C4.

- k2 = P(C2=1|q4=0, q5=1, q6=0) = 0.081
- k3 = P(C3=1|q7=1, q8=0, q9=1) = 0.300
- k4 = P(C4=1|q10=1, q11=1, q12=0) = 0.394

As mentioned, we use k1,...,k4 as value of learner’s knowledge in concepts C1,...,C4. And because these are probability values, they will be a number between 0 and 1.

Finally, as C1, C2, C3, and C4 are independent; $k_1 \times k_2 \times k_3 \times k_4$ is used to compute the whole learner's knowledge.

C. OPEN LEARNER MODELING

After modeling learner's knowledge, the model was shown to learners as Fig.4. The first column shows the concepts, and the second column shows the value of $k_1, k_2, k_3,$ and $k_4,$ numerically and also as skill meter.

After observing the measured knowledge's value in individual concepts, each learner could express his/her belief about each concept's value in the last column. S/he may agree with the calculated knowledge's value or believe that her/his knowledge in each concept is more or less than what is shown. For example Fig.4 shows 0.257 ($=k_1$) as a learner's knowledge in concept C1. Suppose the learner believes that his/her knowledge in concept C1 is a number like 0.7, so s/he could enter the new value in third column. The learner's belief about different concepts should be entered as a number between 0 and 1.

Concepts:	Your Knowledge in System	Your Idea About Your Knowledge
Add and Delete in Link List	0.257	<input type="text"/>
Scan and Use of Link List	0.821	<input type="text"/>
Time Order	0.312	<input type="text"/>
Push and Pop and Use of Stack	0.732	<input type="text"/>

Fig. 4. Opening model of learner

D. UPDATING LEARNER MODEL WITH PROPOSED METHOD

In this state, considering the learner's belief, the value of learner's knowledge is updated as follow:

$$k'_i = k_i + \frac{(LB_i - k_i)}{k_i + 1} \tag{5}$$

In this formula:

- K_i : The value of learner's knowledge in concept C_i ($i \in \{1, \dots, 4\}$).
- LB_i : The learner belief about his/her knowledge in concept C_i (the values of the third column).
- K'_i : The value of learner's knowledge that is computed by formula 5.

For instance if the calculated value of a learner's knowledge in C1 is 0.65, and his/her belief about his/her knowledge's value is 0.8, using formula 5 the knowledge's value is updated:

$$K'_1 = 0.65 + (0.8-0.65) / (0.65+1) = 0.74$$

Actually, updating is based on the learner belief and the calculated value of knowledge in the previous step. Using this update, we aim to increase the accuracy of the calculated value of learner's knowledge and in fact, learner model.

Taking a Comprehensive Test: After updating learner model by means of proposed method (formula 5), we tried to evaluate the accuracy of updated learner model. For this purpose, we took a comprehensive test and compared the knowledge value that was obtained by this test and knowledge value that was obtained by formula 5. The comprehensive test includes 10 questions that each question is related to a C_i . We used T_i to refer to knowledge value in concept C_i that has been obtained by comprehensive test.

E. ANALYZING THE RESULTS

We are going to investigate whether the proposed method and updating model by using learner's belief, has improved the accuracy of knowledge model. For this purpose we studied that the amount of which of knowledge (K'_i or K_i) is closer to result of the comprehensive test. As mentioned K_i and K'_i are the values of learner's knowledge in C_i before and after updating by formula 5.

At first the $T_i - K'_i$ and $T_i - K_i$ were computed. If the difference between T_i and K'_i is less than the difference between T_i and K_i , it seems that our proposed method has improved the accuracy of learner model. We applied student's t-test (t-test) to study whether the result is meaningful. In following subsections t-test and results are explained.

T-test (Student's t-test): Student's t-test, in statistics, is a method of testing hypotheses about the mean of a small sample drawn from a normally distributed population when the population standard deviation is unknown [19]. In simple terms, the t-test compares the actual difference between two means about the variation in the data. There are three types of t-test:

- **One-sample t-test:** Used to compare a sample mean with a known population mean or some other meaningful, fixed value. That is subjects are randomly drawn from a population and the distribution of the mean being tested is normal.
- **Independent samples t-test:** Used to compare two means from independent groups.
- **Paired samples t-test:** This is appropriate for testing the mean difference between paired observations when the paired differences follow a normal distribution. It uses when the observed data are from the same subject and we are going to compare data before-after a situation [20, 21].

We are going to compare accuracy of knowledge model before and after use of proposed method (formula 5), hence we have the same subject (knowledge model) and we should use the Paired samples t-test.



THE RESULTS

As mentioned, we aim to use Paired t-test to show that the proposed method has improved the accuracy of learner model. In other words, we should show that K_i' to compare K_i is closer to T_i , or T_i-K_i' is less than T_i-K_i . And we should also show there is meaningful difference between the means of T_i-K_i' and T_i-K_i . In order to apply t-test, the variables should be normal. We used MiniTab for normality test as well t-test.

Normality test in MiniTab: As stated, we aimed to compare T_i-K_i to T_i-K_i' ($\forall i \in \{1,2,3,4\}$). At first, normality of each T_i-K_i and T_i-K_i' was assessed using MiniTab. For example Fig.5 shows normality test for each T_1-K_1 using MINITAB.

MINITAB generates a normal probability plot and performs a hypothesis test to examine whether the observations follow a normal distribution or not. For this test, the hypotheses are:

H_0 : data follow a normal distribution

Vs. H_1 : data do not follow a normal distribution

The null hypothesis would be rejected as the p-value is less than alpha (α) level, and it means the data is highly non-normal. Note that the p-value is the probability of incorrectly rejecting the null hypothesis.

The alpha is the maximum acceptable level of risk for rejecting a true null hypothesis and is expressed as a probability ranging between 0 and 1. The most commonly used alpha level is 0.05 [15] and in this paper the value of 0.05 is considered as the alpha level.

Fig.5(a) shows the normality test of T_1-K_1 in an enlarged view. As shown in this figure, the mean of T_1-K_1 is 0.4701. The p-value equals 0.193 which is greater than 0.05. So we are unable to reject the null hypothesis, as a result T_1-K_1 is assumed normal. The normality test of all T_i-K_i' and T_i-K_i are shown in Fig.5 (a,...,j).

In each Fig.5 (a,...,j) the straight line on the graph is the null hypothesis of normality. The p-value tells us whether our data are significantly different from this line [16]. We follow the same way to compute the normality of T_2-K_2 , T_3-K_3 , T_4-K_4 , T_1-K_1' , T_2-K_2' , T_3-K_3' , and T_4-K_4' . Table 2 shows the results. The normality test's p-value of all variables is greater than alpha value, so the null hypothesis (of normality test) could not be rejected and all of variables T_i-K_i' and T_i-K_i are normal.

Paired samples t-test in MiniTab: For a paired t-test:

$H_0: \mu_2 = \mu_1$

Vs. $H_1: \mu_2 \neq \mu_1$.

Where μ_2 and μ_1 are mean of T_i-K_i' and T_i-K_i . In other words, H_0 expresses there is no meaningful difference between the means of T_i-K_i' and T_i-K_i ; and H_1 states the difference is significance.

Table2. The Result of Normality Test For T_i-K_i' , T_i-K_i

Variable	Mean Value	P-value From Normality Test	
T_1-K_1'	0.095	0.332	greater than 0.05
T_1-K_1	0.470	0.193	greater than 0.05
T_2-K_2'	0.324	0.456	greater than 0.05
T_2-K_2	0.552	0.295	greater than 0.05
T_3-K_3'	0.405	0,093	greater than 0.05
T_3-K_3	0.492	0.316	greater than 0.05
T_4-K_4'	0. 313	0.213	greater than 0.05
T_4-K_4	0. 520	0.101	greater than 0.05

Based on results, the null hypothesis would be rejected if p-value became less than alpha level. We would fail to reject the null hypothesis if p-value was greater than alpha level and it would conclude that there is meaningful difference in the mean of the two groups [16].

For example, Fig.6(a) states the result of Paired t-test using MINITAB, for T_1-K_1' and T_1-K_1 . The figure shows that the mean value of T_1-K_1' is -0.095 that is less than the mean value of T_1-K_1 (0.470). So it seems proposed method has improved the accuracy of knowledge model. Also the computed p-value is 0.004, which is less than considered alpha value. This small p-value suggests that the data are inconsistent with H_0 , and H_0 is rejected. Therefore the H_1 is confirmed and there is a meaningful difference between two means. So the proposed method has improved the accuracy of knowledge model in concept C1.

We also used T-test for comparing T_2-K_2 to T_2-K_2' , T_3-K_3 to T_3-K_3' , and T_4-K_4 to T_4-K_4' . The results of comparing have shown in Fig.6 (b, c, d). A summarized of T-test results, is shown in Table3.

Table3. The Result of T-test For T_i-K_i' and T_i-K_i

Variables	P-value of Paired T-test	
T_1-K_1' and T_1-K_1	0.004	less than 0.05
T_2-K_2' and T_2-K_2	0.002	less than 0.05
T_3-K_3' and T_3-K_3	0.017	less than 0.05
T_4-K_4' and T_4-K_4	0.063	greater than 0.05

The p-value of Paired t-test for (T_2-K_2' and T_2-K_2) and (T_3-K_3' and T_3-K_3) are less than alpha value, hence the data are inconsistent with H_0 , and H_0 is rejected. Therefore the H_1 is confirmed and there are meaningful differences between two means. As a



result, our proposed method has improved accuracy of learner model in two concepts C2 and C3 same as C1.

The p-value of Paired t-test for (T_4-K_4' and T_4-K_4) is 0.063 that is greater than considered alpha level (0.05). Consequently, we cannot reject the null hypothesis. It means we could not confirm that proposed method could improve the accuracy of knowledge model in concept C4. But if we consider 0.1 as alpha level (it means we accept more risk to reject a true null hypothesis) the value 0.063 is less than 0.1 and the null hypothesis (H_0 of Paired t-test) will be rejected. Therefore our proposed method would improve the accuracy of knowledge model in concept C4.

In this survey, in addition of C₁, C₂, C₃, and C₄, another concept had been considered, but since the values of T_1-K_1' for this concept was non-normal, we could not rely on the Paired t-test of this concept. So we ignored this concept.

IV. CONCLUSION

As mentioned the accuracy of learner model is an important issue. Open learner modeling is an approach which is used for this aim. In this paper a novel method was proposed to improve accuracy of learner model based on learner knowledge and learner belief. For this purpose the knowledge model of 16 students in 4 concepts of Data Structure and Algorithms lesson, were obtained and represented by use of the overlay learner modeling using Bayesian Networks. Then we presented the learner model as skill meter and learner stated his/her belief about it. Then the model was updated through a proposed method. At last we took a comprehensive test to evaluate our method. Since we were going to compare the knowledge model before and after applying our proposed method, we used Paired t-test. For this idea

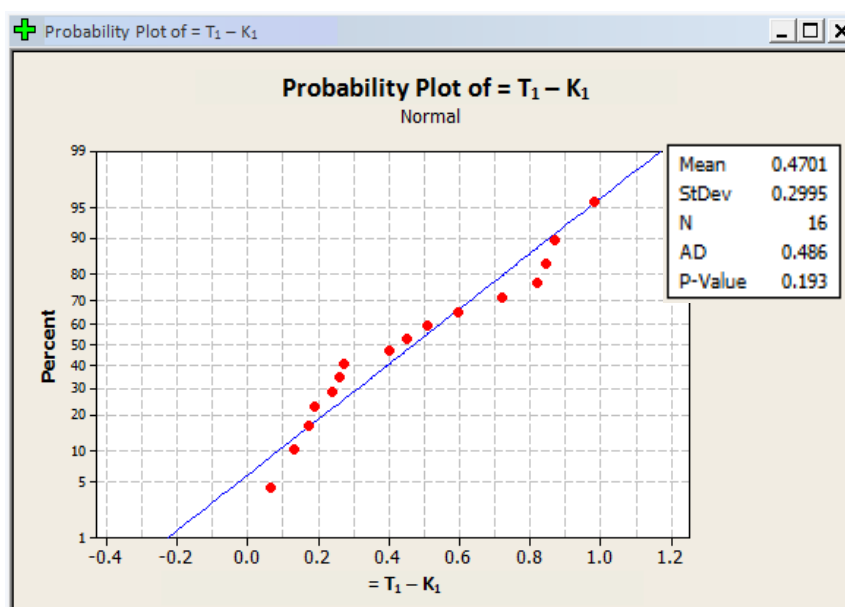
we applied Paired t-test in MINITAB to compare the mean of difference between comprehensive test and updated knowledge model (computed by proposed method) on the one hand and the mean of difference between comprehensive test and knowledge model (before update) on the other hand. The obtained results have shown that for three concepts the p-value of Paired t-test is less than 0.05(alpha value=0.05) and for one concept the p-value is less than 0.1(alpha value=0.1). It means for selected concepts our method have improved the accuracy of learner model.

As future works, we are going to develop our method by following capacity:

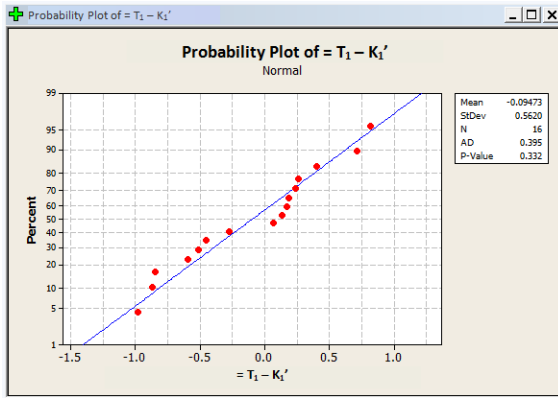
To make use of other parameters of learner model: As mentioned, learner model has several parameters such as emotions, background, and individual traits. In this study we used knowledge model. We are going to apply other parameters to improve our method.

To negotiate with learner about his/her belief on his/her learner model: It means when learner expresses his/her idea about his/her learner model, system negotiates with the learner to assess the truth of learner idea, and then learner model is updated. To assess accuracy of learner belief, system could use other questions about related concept, and then based on answer decides whether update learner model or not.

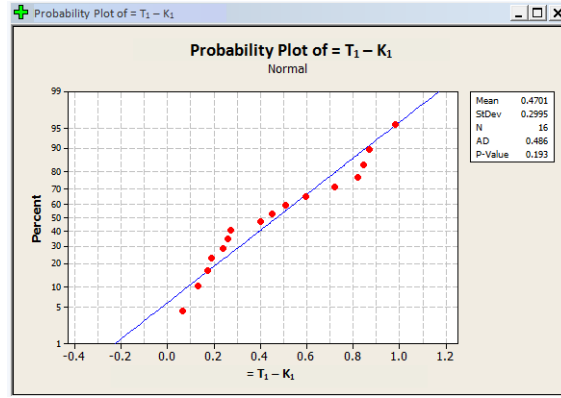
To follow a line of investigation about learning contents: According to table 2, the difference between mean of T_1-K_1' and T_1-K_1 , in variant concepts is different. The third concept (C₃) is mathematical, and it has minimum difference mean of T_3-K_3' and T_3-K_3 . So the type of concept could be considered as another parameter of proposed method.



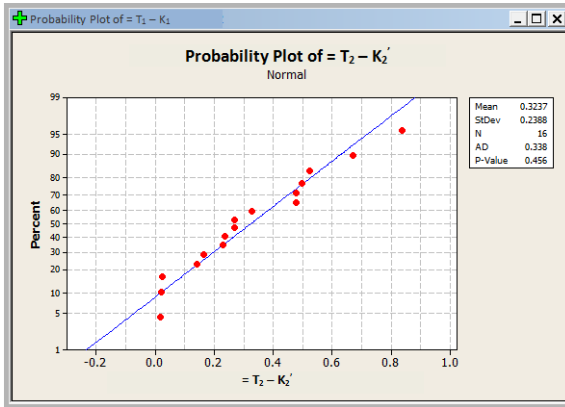
a: Normality Test for T_1-K_1 (In an enlarged view)
(P-value= 0.193)



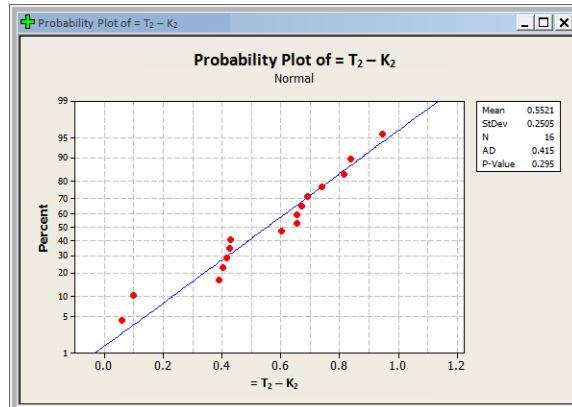
b: Normality Test for $T_1 - K_1'$ (P-value= 0.332)



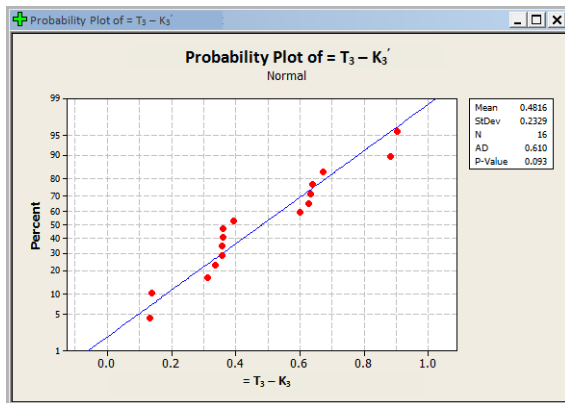
c: Normality Test for $T_1 - K_1$ (P-value= 0.193)



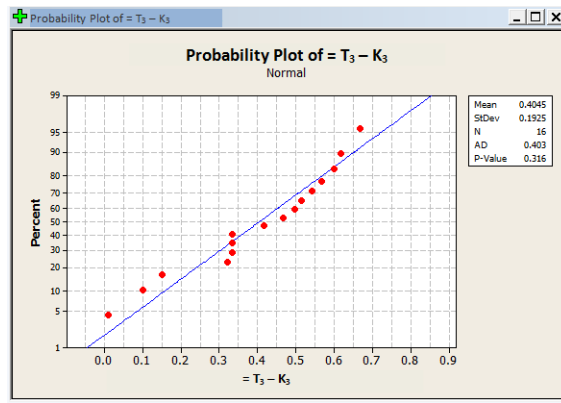
d: Normality Test for $T_2 - K_2'$ (P-value= 0.456)



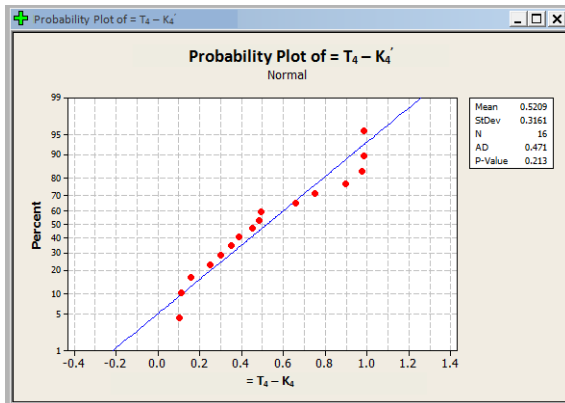
e: Normality Test for $T_2 - K_2$ (P-value= 0.295)



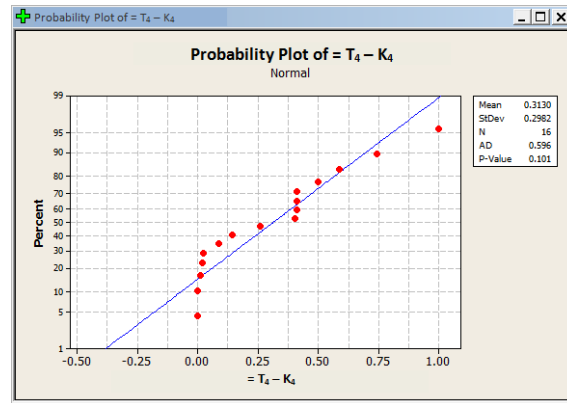
g: Normality Test for $T_3 - K_3'$ (P-value= 0.093)



h: Normality Test for $T_3 - K_3$ (P-value= 0.316)



i: Normality Test for $T_4 - K_4'$ (P-value= 0.213)



j: Normality Test for $T_4 - K_4$ (P-value= 0.101)

Fig. 5. Normality Test in MINITAB

Paired T for = $T1-K_1' - T1-K_1$

	N	Mean	StDev	SE Mean
= $T1-K_1'$	16	-0.095	0.562	0.141
= $T1-K_1$	16	0.470	0.300	0.075
Difference	16	-0.565	0.738	0.184

95% upper bound for mean difference: -0.241
T-Test of mean difference = 0 (vs < 0): T-Value = -3.06 P-Value = 0.004

(a) T-test Result for T_1-K_1' and T_1-K_1

Paired T for = $T2-K_2' - T2-K_2$

	N	Mean	StDev	SE Mean
= $T2-K_2'$	16	0.3237	0.2388	0.0597
= $T2-K_2$	16	0.5521	0.2505	0.0626
Difference	16	-0.2283	0.2765	0.0691

95% upper bound for mean difference: -0.1071
T-Test of mean difference = 0 (vs < 0): T-Value = -3.30 P-Value = 0.002

(b) T-test Result for T_2-K_2' and T_2-K_2

Paired T for = $T3-K_3' - T3-K_3$

	N	Mean	StDev	SE Mean
= $T3-K_3'$	16	0.4045	0.1925	0.0481
= $T3-K_3$	16	0.4920	0.1766	0.0442
Difference	16	-0.0875	0.1505	0.0376

95% upper bound for mean difference: -0.0215
T-Test of mean difference = 0 (vs < 0): T-Value = -2.33 P-Value = 0.017

(c) T-test Result for T_3-K_3' and T_3-K_3

Paired T for = $T4-K_4' - T4-K_4$

	N	Mean	StDev	SE Mean
= $T4-K_4'$	2 16	0.5209	0.3161	0.0790
= $T4-K_4$	16	0.3130	0.2982	0.0745
Difference	16	0.208	0.414	0.104

95% CI for mean difference: (-0.013, 0.429)
T-Test of mean difference = 0 (vs not = 0): T-Value = 2.01 P-Value = 0.063

(d) T-test Result for T_4-K_4' and T_4-K_4

Fig. 6. T-test Result for T_i-K_i' and T_i-K_i

REFERENCES

- [1] Brusilovsky, P. & Millán, E. (2007): "User models for adaptive hypermedia and adaptive educational systems". In Brusilovsky, P., Kobsa, A. & Neid, W. (Eds.), *The Adaptive Web: Methods and Strategies of Web Personalization* (PP. 3-53), PA: Berlin Heidelberg New York: Springer-Verlag.
- [2] Desmarais, M. C., & d Baker, R. S. (2012). A review of recent advances in learner and skill modeling in intelligent learning environments. *User Modeling and User-Adapted Interaction*, 22(1-2), 9-38
- [3] Bull, S. & Kay, J. (2010). Open Learner Models, in R. Nkambou, J. Bordeau & R. Miziguchi (eds), *Advances in Intelligent Tutoring Systems*, Springer, 318-338.
- [4] HSIAO, I.-H., BAKALOV, F., BRUSILOVSKY, P., & NIGRIES, B. K. (2013). Progressor: social navigation support through open social student modeling *New Review of Hypermedia and Multimedia*, 19(2), 112-131. doi: 10.1080/13614568.2013.806960
- [5] Bull, S., H. Pain, and I. University of Edinburgh. Dept. of Artificial, "Did I Say What I Think I Said, and Do You Agree with Me?": Inspecting and Questioning the Student Model. DAI RESEARCH PAPER, 1995.
- [6] Zapata-Rivera, D. and J. Greer."Exploring various guidance mechanisms to support interaction with inspectable learner models". 2002: Springer.
- [7] Kerly, A., P. Hall, and S. Bull, (2007),"Bringing chatbots into education: Towards natural language negotiation of open learner models". *Knowledge-Based Systems*, 20(2): p. 177-185.
- [8] Bull, S., Gardner, P., Ahmad, N., Ting, J. & Clarke, B. (2009). Use and Trust of Simple Independent Open Learner Models to Support Learning Within and Across Courses, in G.-J. Houben, G. McCalla, F. Pianesi & M. Zancanari (eds), *User Modeling, Adaptation and Personalization*, Springer-Verlag, Berlin Heidelberg,42-53.
- [9] Brusilovsky, P. (1996): "Adaptive hypermedia, an attempt to analyze and generalize". In Brusilovsky, P., Kommers, P., Streitz, N. (Ed.): *Multimedia, Hypermedia, and Virtual Reality*. Lecture Notes in Computer Science (288-304), PA: Springer-Verlag, Berlin
- [10] Brajnik, G., Guida, G. & Tasso, C. (1987): "User Modeling in Intelligent Information Retrieval". *Information Processing & Management*, 23, 305-320.
- [11] De Bra, P. & Ruiter, J.-P. (2001): "AHA! Adaptive hypermedia for all". In Fowler, W., Hasebrook, J. (Ed.) *Proc. of WebNet'2001*, World Conference of the WWW and Internet (pp. 262-268).
- [12] Botman, A. M. Kok, A. J. & Siklossy, L. (1989): "Methods for User Modelling in an Intelligent Interface for Data Retrieval". Unpublished Manuscript, Department of Mathematics and Computer Science, Free University, Amsterdam, Netherlands.
- [13] Heckerman, D., (1995), "A Tutorial on Learning With Bayesian Networks", Technical Report (MSR-TR-95-06), <http://research.microsoft.com/apps/pubs/default.aspx?id=69588>.
- [14] Murray, R.C., VanLehn, K. & Mostow, J. (2004). "Looking ahead to select tutorial actions: A decision-theoretic approach". *International Journal of Artificial Intelligence in Education*, 14(3-4), 235-278.
- [15] Mislavy, R.J., Almond, R.G., Yan, D., & Steinberg, L.S. (1999). "Bayes nets in educational assessment: Where do the numbers come from?" In K.B. Laskey & H.Prade (Eds.), *Proceedings of the Fifteenth Conference*
- [16] Sabourin, J., Mott, B., & Lester, J. (2013). Utilizing Dynamic Bayes Nets to Improve Early Prediction Models of Self-regulated Learning. In *User Modeling, Adaptation, and Personalization* (pp. 228-241). Springer Berlin Heidelberg.
- [17] Bull, S., Kay, J.: Open Learner Models. In (2010): in R. Nkambou, J. Bordeau & R. Miziguchi (eds), *Advances in Intelligent Tutoring System*, 318-338, Springer-Verlag Berlin, Morales, R.
- [18] Bull, S. and Kay, J. (2006) "Student Models that Invite the Learner In: The SMLIJ Open Learner Modelling Framework". Technical Report, University of Sydney, Australia, TR 580.
- [19] Student's t-test. (2011). In *Encyclopædia Britannica*. Retrieved from <http://www.britannica.com/EBchecked/topic/569907/Students-t-test>
- [20] By Keith M. Bower, M.S., *The Paired T-Test Using MINITAB*, http://www.MiniTab.com/uploadedFiles/Shared_Resources/Documents/Articles/paired_t_test.pdf
- [21] *Statistical Inference and t-Tests*, MiniTab Inc, <http://www.MiniTab.com>



Ahmad A. Kardan, received his B.Sc. in Electrical Engineering from Sharif University of Technology (1976-Iran), his M.Sc. in Digital Systems from the Brunel University (1997-UK), and his Ph.D. in Electrical Engineering from Imperial College of Science and Technology (2001-UK). He is currently a faculty member and director of The Advanced E-Learning Technologies Laboratory (AELT-Lab) of the Computer Engineering Department, at Amirkabir University of Technology, Tehran, Iran. He Founded The Virtual Education Center of Amirkabir University of Technology in 2002. He teaches graduate courses in computing and information technology with emphasis on advanced e-learning and distributed educational systems. Dr. Kardan is involved in researches in Intelligent Tutoring Systems (ITS), Collaborative Learning, Concept Mapping, Learning Advisory Systems, Learner Modeling, Adaptive Learning, Self-Regulated Learning, Recommender Systems for e-Learning Environments, Knowledge Management, and Applying Data Mining in e-Learning Environments. He has presented more than 80 papers at national and international conferences, journals and as chapters for related books.



Seyede Fatemeh Noorani, received her B.Sc. in Mathematics from Iran University of Science & Technology (2000-Iran) and her M.Sc. in Computer Engineering from Shahid Beheshti University (2002-Iran). She is currently a faculty member of Computer Engineering, at Payame Nour University. She is involved in researches in E-learning, Learning Styles, Learner Modeling and Collaborative Learning.



Somayeh Modaberi received her B.Sc. in Computer science from Tabriz (2007-Iran), and her M.Sc. in Electronic Commerce from the Amirkabir University (2011). She is a post graduate researcher and a member of The Advanced E-Learning Technologies Laboratory (AELT-Lab), Computer Engineering Department, at Amirkabir University of Technology, Tehran, Iran. Ms.Modaberi is involved in researches in different domains related to E-Learning, User Molding and Social Networks.

