# A Novel DS-CDMA Direction of Arrival Estimator for Frequency- Selective Fading Channel with Correlated Multipath by Using Beamforming Filter 

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#### Abstract

In this paper, a new method for estimating the direction of arrival of Asynchronous DS-CDMA signals in multipath fading channel is proposed. In the proposed method, first, for removing the effects of undesired paths, we project the coherent signals of the undesired paths perpendicularly to the under process signal, next, the signal is passed through a filter bank.Byusing beam forming filters, the effectof other users on the desired users signal is decreased and hence, the search area is decreased almost to one tenth. In this algorithm, searching all angles is not required,to estimate the number of sources does not require any information criteria, andalso, the number of users can exceed the number of antenna arrays contrary to many of the conventional methods. Simulation results are illustrated to confirm the efficiency of the method.


Keywords; Direction of arrival estimation, orthogonal projection, beam forming, frequency-selective fading channel.

## I. Introduction

The system capacity can be increased by using temporal or spatial signal processing techniques to transmit and receive signals. The smart antenna techniques, including beamforming and diversity ones, are especially useful in mobile direct-sequence code division multiple access (DS-CDMA) communication systems [1].

Here, we consider the state that a beamforming array is adopted at the base station while each mobile user transmits the signal by using a single antenna. In such a system, direction of arrival (DOA) of the received signals is a parameter for the base station to be estimated, in order to set up reliable connection for data transmission among mobile users. The DOAs of users are not available in practice and should be estimated for implementation of optimum receivers.

Furthermore in recent years, estimating the direction of arrival has been an attractive area of research because of its important application in radar and wireless location finding. Among the proposed methods, the signal subspace algorithms have attracted a lot of interest due to their high resolution. However, in a highly correlated or coherent environment due to multipath propagation, the direction of coherent signals cannot be detected via conventional subspace methods like the MUltipleSIgnal Classification (MUSIC) algorithmandEstimation of Signal Parameters via Rotational Invariance Techniques(ESPRIT),since the spatial signatures cannot be resolved in the signal subspace [2-4].

Furthermore, in order to estimate DOA by conventional methods, the number of array elements must be greater than the number of users; this is impractical in CDMA systems with a large number of active users. A DOA estimator employing code matched filters and parallel MUSIC is proposed in [5]. In this method other users except of active users are considered Gaussian noise and as aninterference. In [6] a subspace method for estimating DOA for multiple coherent narrowband signals is proposed.

In this paper, we propose a method for DS-CDMA signal DOA estimation with an array of antennas at the receiver. First, we decorrelate the received signal of each path by orthogonal projection and then apply a bank of $2 M$ ( $M$ is the number of arrays) beam forming filters to the received two-dimensional (2-D) signal which results in $2 M$ time domain sequences. The total energy of interfering signals is reduced after each beam forming filter. The energy of desired signalis also reduced, since the DOA is still unknown at this stage. However, the proposed algorithm, together with this receiver structure is able to control the loss of energy while maintaining the SNR level.

The paper is organized as follows. In Section II, we describe the mathematical model of the system, set the underlying assumptions and define the problem objectives. In Section III, the proposed method is developed for synchronous single path and asynchronous multipath cases. In Section IV, performance of the proposed method is evaluated by simulation, and Section V concludes the paper.

## II. Mathematical model

## A. Notation

The notations employed in this paper are standard. Signals are discrete-time and complex in general. Upper and lower-case bold letters denote matrices and vectors, respectively. The operators $(\square)^{T}$ and $(\square)^{H}$ denote transpose and hermitianoperationsrespectively. Finally $\otimes$ isKronecker matrix product.

## B. System Model

Consider a DS-CDMA system with $K$ active users transmitting binary information sequences of
$b_{1}, b_{2}, \ldots, b_{K}$ with normalized spreading waveforms $s_{1}, s_{2}, \ldots, s_{K}$ that are randomly distributed in space. A $Q$ bit transmitted baseband signal from the $k$-th user is:

$$
\begin{align*}
& x_{k}(t)=A_{k} \sum_{i=0}^{Q-1} b_{k}(i) s_{k}\left(t-i T_{b}\right)  \tag{1}\\
& k=1,2, \ldots ., K
\end{align*}
$$

Where $T_{b}$ is the bit interval, $b_{k}(i) \in\{-1,+1\}$ is the $i$-th bit of a sequence of independent and identically distributed(i.i.d) random variables transmitted by the $k$ $t h$ user and $A_{k}$ denotes the amplitude of the $k$-th user. $s_{k}(t)$ is defined as follows and its energy is limited to $\left[0, T_{b}\right]:$
$s_{k}(t)=\sum_{j=0}^{N_{c}-1} c_{k}(j) \psi\left(t-j T_{c}\right) \quad 0 \leq t \leq T_{b}$
where $N_{c}=T_{b} / T_{c}$ is the processing gain; and $\psi(t)$
is a chip waveform of duration $T_{c}$ and $\left\{c_{k}(n)\right\}_{n=1}^{n=N_{c}-1}$ is a signature code sequence of $\pm 1 \mathrm{~s}$ assigned to the $k$ - $t h$ user that can be represented as $\underline{c}_{k}=\left[\begin{array}{llll}c_{k}(0) & c_{k}(1) & \ldots . & c_{k}\left(N_{c}-1\right)\end{array}\right]^{T}$.

At the receiver, an antenna array of $M$ elements is employed and the baseband multipath channel of the $k$ th user can be modeled as a single-input multipleoutput channel with $M \times 1$ vector impulse response $\underline{h}_{k}(t)$ given as [5]

$$
\begin{equation*}
\underline{h}_{k}(t)=\sum_{l=1}^{L} g_{k l} \delta\left(t-\tau_{k l}\right) \underline{\theta}_{\theta_{k l}} \tag{3}
\end{equation*}
$$

where $L$ is the number of paths in each user's channel, $g_{k l}$ and $\tau_{k l}$ are gain and delay of the l-th path of the $k$-th user's signal respectively, $\delta($.$) is the$ Dirac delta function and $\underline{a}_{\theta_{k l}}=\left[a_{1}^{\theta_{k l}}, \ldots, a_{M}^{\theta_{k l}}\right]^{T}$ is the array response vector corresponding to the $l$-th path of the $k$-th user's signal with DOA of $\theta_{k l}$.

Thetotal received baseband signal at the i-th antenna denoted by $r_{i}(t)$ is the superposition of the signals from all users plus the additive ambient noise and the $M \times 1$ vector $\underline{r}(t)=\left[r_{1}(t), \ldots, r_{M}(t)\right]^{T}$ can be expressed as:

$$
\begin{align*}
& \underline{r}(t)=\sum_{k=1}^{K} x_{k}(t) * \underline{h}_{k}(t)+\sigma \underline{n}(t) \\
& =\sum_{i=0}^{Q-1} \sum_{k=1}^{K} A_{k} b_{k}(i) \sum_{l=1}^{L} \underline{a}\left(\theta_{k l}\right) g_{k l}  \tag{4}\\
& \times s_{k}\left(t-i T_{b}-\tau_{k l}\right)+\sigma \underline{n}(t)
\end{align*}
$$

where * denotes convolution, $\sigma^{2}$ is the variance of the ambient noise at each antenna element and $\underline{n}(t)=\left[n_{1}(t), \ldots, n_{M}(t)\right]^{T}$ is a vector of independent
zero mean complex white Gaussian noise processes with unit variance, i.e.

$$
\begin{equation*}
E\left\{\underline{n}(t) \underline{n}\left(t^{\prime}\right)^{H}\right\}=I_{M} \delta\left(t-t^{\prime}\right) \tag{5}
\end{equation*}
$$

Where $E$ is the expectation operator and $I_{M}$ is the $M \times M$ identity matrix. We also assume that the noise processes and transmitted sequences of users are statistically independent.

To find the directions of the received signals from the $l$-th path of the $k$-th user, the receiver's chip matched filter is synchronized with the delay of $\tau_{k l}$. The receiver works at the discretechip rate.The sample of $m$-th antenna is:
$y_{k l, m}(i, j)=$

$$
\begin{equation*}
\int_{i T_{b}+\tau_{k l}+j T_{c}}^{i T_{b}+\tau_{k}+(j+1) T_{c}} r_{m}(t) \psi^{*}\left(t-i T_{b}-\tau_{k l}-j T_{c}\right) d t \tag{6}
\end{equation*}
$$

$M$ samples of antenna output can be represented by a $M \times 1$ vector as:

$$
\underline{y}_{k l}(i, j)=\left[\begin{array}{c}
y_{k l, 1}(i, j)  \tag{7}\\
y_{k l, 2}(i, j) \\
\vdots \\
y_{k l, M}(i, j)
\end{array}\right]
$$

Or:

$$
\underline{y}_{k l}(i, j)=\left[\begin{array}{c}
y_{k l, 1}(i, j)  \tag{8}\\
y_{k l, 2}(i, j) \\
\vdots \\
y_{k l, M}(i, j)
\end{array}\right]=
$$

$\int_{i T_{b}+\tau_{l l}+j T_{c}}^{i T_{b}+\tau_{k}+(j+1) T_{c}} \underline{r}(t) \psi^{*}\left(t-i T_{b}-\tau_{k l}-j T_{c}\right) d t$
By combining thevectors $\underline{y}_{k l}$, we define the $M \times N_{c}$ matrix $B L_{k l}(i)$ as follows:

$$
\begin{align*}
& B L_{k l}(i)= \\
& {\left[\underline{y}_{k l}(i, 0), \underline{y}_{k l}(i, 1), \ldots, \underline{y}_{k l}\left(i, N_{c}-1\right)\right]} \tag{9}
\end{align*}
$$

The contribution of $k$-th user at $m$-th antenna $\left(r_{m}(t)\right.$ ) is:
$r_{m}^{k}(t)=$
$A_{k} \sum_{q=0}^{Q-1} b_{k}(i) \sum_{l=1}^{L} g_{k l} a_{m}\left(\theta_{k l}\right) s_{k}\left(t-q T_{b}-\tau_{k l}\right)$

Therefore the contribution of $k$-th user at $y_{k l, m}(i, j)$ is:

$$
\begin{aligned}
& B L_{k l, m}^{k}(i)=y_{k l, m}^{k}(i, j) \quad 0 \leq j \leq N_{c}-1 \\
& \quad=A_{k} \sum_{q=0}^{Q-1} b_{k}(q) \sum_{p=1}^{L} g_{k p} a_{m}\left(\theta_{k p}\right) \\
& \times \int_{i T_{b}+j T_{c}+\tau_{k l}}^{i T_{b}+\left(j+1 T_{c}+\tau_{k l}\right.} s_{k}\left(t-q T_{b}-\tau_{k p}\right) \psi^{*}\left(t-i T_{b}-j T_{c}-\tau_{k l}\right) d t
\end{aligned}
$$

(11)

Due to $\psi(t)$ waveform at $\left[0, T_{c}\right]$ and $s_{k}(t)$ at $\left[0, T_{b}\right]$, product of $s_{k}\left(t-q T_{b}-\tau_{k p}\right)$ and $\psi\left(t-i T_{b}-j T_{c}-\tau_{k l}\right)$ is always zero except in two cases:

$$
\begin{gather*}
i T_{b}+j T_{c}+\tau_{k l}+T_{c} \geq q T_{b}+\tau_{k p}  \tag{12}\\
i T_{b}+j T_{c}+\tau_{k l}<q T_{b}+\tau_{k p}+T_{b} \tag{13}
\end{gather*}
$$

Since the effect of $i-1, i, i+1$-th bits in integral, $y_{k l, m}^{k}(i, j)$ simplifies to:

$$
\begin{align*}
& y_{k l, m}^{k}(i, j)= \\
& A_{k} b_{k}(i-1) \sum_{p=1}^{L} g_{k p} a_{m}\left(\theta_{k p}\right) \underline{c}_{k p}^{l,-1} \\
& +A_{k} b_{k}(i) \sum_{p=1}^{L} g_{k p} a_{m}\left(\theta_{k p}\right) \underline{c}_{k p}^{l, 0}  \tag{14}\\
& +A_{k} b_{k}(i+1) \sum_{p=1}^{L} g_{k p} a_{m}\left(\theta_{k p}\right) \underline{c}_{k p}^{l,+1}
\end{align*}
$$

Where $\underline{c}_{k p}^{l, s}$ is a $1 \times N_{c}$.

$$
\underline{c}_{k p}^{l, s}=\left[c_{k p}^{l, s}(0), c_{k p}^{l, s}(1), \ldots, c_{k p}^{l, s}\left(N_{c}-1\right)\right]
$$

$c_{k p}^{l,-1}=\int_{j T_{c}+\tau_{k l}}^{(j+1) T_{c}+\tau_{k l}} s_{k}\left(t+T_{b}-\tau_{k p}\right) \psi^{*}\left(t-j T_{c}-\tau_{k l}\right) d t$
$c_{k p}^{l, 0}=\int_{j T_{c}+\tau_{k l}}^{(j+1) T_{c}+\tau_{k l}} s_{k}\left(t-\tau_{k p}\right) \psi^{*}\left(t-j T_{c}-\tau_{k l}\right) d t$
$c_{k p}^{l,+1}=\int_{j T_{c}+\tau_{k l}}^{(j+1) T_{c}+\tau_{k l}} s_{k}\left(t-T_{b}-\tau_{k p}\right) \psi^{*}\left(t-j T_{c}-\tau_{k l}\right) d t$

As a result, the contribution of $n$-th user at $B L(i)$ matrix is:

$$
\begin{align*}
& B L_{k l}^{k}(i)=A_{k} b(i-1) \sum_{p=1}^{L} g \underline{a}\left(\theta_{k p}\right) \otimes \underline{c}_{k p p}^{l,-1} \\
& +A_{k} b(i) \sum_{p=1}^{L} g \underline{a}\left(\theta_{k p}\right) \otimes \underline{c}_{k p}^{l, 0}  \tag{19}\\
& +A_{k} b(i+1) \sum_{p=1}^{L} g \underline{a}\left(\theta_{k p}\right) \otimes \underline{c}_{k p}^{l,+1}
\end{align*}
$$

## III. THE PROPOSED METHOD

## A. Proposed method for synchronous single path case

First we consider the case where all users are transmitting synchronously in a single path fading system, i.e. $L=1$. Without loss of generality, assume $\tau_{1}=\tau_{2}=\ldots=\tau_{K}$. In this case $B L$ matrix is independent of indices $k$ and $l$ and simplifies to:

$$
\begin{equation*}
B L_{k l}^{k}(i)=A_{k} b_{k}(i) g_{k} \underline{a}\left(\theta_{k}\right) \otimes \underline{c}_{k} \tag{20}
\end{equation*}
$$

A bank of $2 M$ beamforming filters $W_{s}$ is applied to $B L$. The beamforming filterbank $W_{s}$ is in the formof $\left[\underline{w}_{s, 1}, \underline{w}_{s, 2}, \ldots, \underline{w}_{s, 2 M}\right]$, where it has $M \times 2 M$ dimension. Each beamforming filter steers at a different direction. The normalized $m$-th beamforming is set up as:

$$
\begin{equation*}
\underline{w}_{s, m}=\frac{1}{M}\left[1, e^{-j \pi \frac{(m-1)}{M}}, \ldots, e^{-j \pi \frac{(M-1)(m-1)}{M}}\right]^{T} \tag{21}
\end{equation*}
$$

which steers at $\sin \theta=m-1 / M$ for $1 \leq m \leq M+1$ or $\sin \theta=\frac{m-1-2 M}{M}$ as $m>M+1$. The example of $\mathrm{M}=2$ is shown in Fig. 2.

The filter output has $2 M \times M$ dimension :
$X=W_{s}{ }^{H} B L(i)=\left[\begin{array}{c}\underline{w}_{s, 1}^{H} B L(i) \\ \vdots \\ \underline{w}_{s, 2 M}^{H} B L(i)\end{array}\right]=$
$\left[\begin{array}{lll}x_{1} & \cdots & x_{2 M}\end{array}\right]^{T}$
The filter response for direction of $k$ - $t h$ user is:

$$
\begin{equation*}
\underline{\Gamma}_{k}=W_{s}^{H} \underline{a}\left(\theta_{k}\right) \tag{23}
\end{equation*}
$$

And if we use uniform linear array (ULA) antenna, then:

$$
\underline{\Gamma}_{k}=\frac{1}{M^{2}}\left[\begin{array}{c}
\sum_{v=0}^{M-1} e^{-j v \pi \sin \theta}  \tag{24}\\
\vdots \\
\sum_{v=0}^{M-1} e^{-j v \pi\left(\sin \theta-\frac{2 M-1}{M}\right)}
\end{array}\right]
$$

The signal in $i$-th block is:

$$
\begin{equation*}
S W=\sum_{k=1}^{K} A_{k} g_{k} \underline{\Gamma}_{k} d_{k}(i) \underline{c}_{k}^{T} \tag{25}
\end{equation*}
$$

If the direction of $k$ - $t h$ user is desired, by assuming:

$$
\begin{cases}E\left[d_{k}\left(j_{1}\right) d_{k}\left(j_{2}\right)\right]=0 & j_{1} \neq j_{2}  \tag{26}\\ E\left[d_{k}\left(j_{1}\right) d_{m}\left(j_{2}\right)\right]=0 & k \neq m\end{cases}
$$



Figure 1. The beam shape at space-doamin for the 2-antenna case: the power response from all beamforming filters

The correlation matrix for the $m$-th row (i.e. the $m$-th beam forming filter output) is:

$$
\begin{equation*}
R_{m}=E\left\{\underline{x}^{H}\right\}=E\left\{\underline{x}_{m}^{T} \underline{x}_{m}^{*}\right\} \tag{27}
\end{equation*}
$$

Where:
$\underline{x}_{m}=\sum_{k=1}^{K} A_{k} g_{k} d_{k}(i) \sum_{v=0}^{M-1} e^{-j \pi v\left(\sin \theta_{k}-\frac{m-1}{M}\right)} \underline{c}_{k}^{T}$
Thus:
$R_{m}=\left(\sum_{k=1}^{K} A_{k} g_{k} d_{k}(i) \Gamma_{k, m} \underline{c}_{k}\right)\left(\sum_{k=1}^{K} A_{k} g_{k} d_{k}(i) \Gamma_{k, m}^{*} \underline{c}_{k}^{T}\right)$ (29)

Where:

$$
\begin{equation*}
\Gamma_{k, m}=\sum_{v=0}^{M-1} e^{-j \pi v\left(\sin \theta_{k}-\frac{m-1}{M}\right)} \tag{30}
\end{equation*}
$$

$(e, f)$-th element of this matrix is:

$$
\begin{align*}
& \left\{A_{1} g_{1} d_{1}(i) \Gamma_{1, m} c_{1}(e)+A_{2} g_{2} d_{2}(i) \Gamma_{2, m} c_{2}(e)+\ldots+\right. \\
& \left.A_{K} g_{K} d_{K}(i) \Gamma_{K, m} c_{K}(e)\right\} \times \\
& \left\{A_{1} g_{1} d_{1}(i) \Gamma_{1, m}^{*} c_{1}(f)+A_{2} g_{2} d_{2}(i) \Gamma_{2, m}^{*} c_{2}(f)+\ldots+\right.  \tag{31}\\
& \left.A_{K} g_{K} d_{K}(i) \Gamma_{K, m}^{*} c_{K}(f)\right\}
\end{align*}
$$

$R_{m}$ stands for the MAI plus noise covariance matrix:

$$
\begin{equation*}
R_{m}=R_{\underline{N}, m}+\left|A_{k} g_{k} \underline{\Gamma}_{k, m}\right|^{2} \underline{c}_{k} \underline{c}_{k}^{T} \tag{32}
\end{equation*}
$$

The direction finding algorithm first identifies a section that the desired signal may fall in. To determine the desired section, we use the largest responses belonging to the beam forming filter. Table I and fig. 1 show the mapping for the 2 -antenna system. To achieve this goal, we use the following function that is constructed for each row [7]:

$$
\begin{equation*}
\varphi_{m}=\frac{1}{\underline{c}_{k}^{T} R_{m}^{-1} \underline{c}_{k}} \tag{33}
\end{equation*}
$$

Now we can compute equation 33 for each rowthen select two largest values of them named $M 1$ and $M 2$. For a given $\sin \theta$ value in the desired section, we can have two response values into a vector representation as:
$\underline{b}_{s}(\sin (\theta))=\frac{1}{M^{2}}\left[\begin{array}{l}\left|\sum_{v=0}^{M-1} e^{-j \pi v \sin (\theta)}\right|^{2} \\ \left|\sum_{v=0}^{M-1} e^{-j \pi v\left(\sin (\theta)-\frac{1}{M}\right)}\right|^{2}\end{array}\right]$
Where $\sin \theta$ ranges from 0 to $1 / 2 M$. After identification of target section, a fine search is performed. $\underline{b}_{s}(\sin (\theta))$ can be treated as a steering vector to search in the range $\sin \theta=0 \sim 1 / 2 M$. By collecting the two largest soft values from (33) to form a vector and constructing an orthogonal projector, we obtain:

$$
\begin{gather*}
\underline{\hat{\varphi}}=\left[\begin{array}{l}
\hat{\hat{\varphi}}_{M 1} \\
\underline{\hat{\varphi}}_{M} 2
\end{array}\right]  \tag{35}\\
P_{\underline{\hat{\varphi}}}=\frac{\hat{\hat{\varphi}} \underline{\hat{\varphi}}^{T}}{\|\hat{\hat{\varphi}}\|^{2}} \tag{36}
\end{gather*}
$$

$\sin (\hat{\theta})=$
$\arg \max _{\sin (\theta)} \frac{\left\|\underline{b}_{s}(\sin \theta)\right\|^{2}}{\underline{b}_{s}(\sin \theta)^{T}\left(I-P_{\hat{\phi}}\right) \underline{b}_{s}(\sin \theta)}$
Let sec stands for the estimated section, then the angle $\theta_{k}$ can be obtained by :
$\hat{\theta}_{k}=\left\{\begin{array}{l}\sin ^{-1}\left(\sin (\hat{\theta})+(\sec -2 M-1) \frac{1}{2 M}\right) \quad \sec \text { is odd } \\ \sin ^{-1}\left(\frac{1}{2 M}-\sin (\hat{\theta})+(\sec -2 M-1) \frac{1}{2 M}\right) \text { sec is even }\end{array}\right.$

## B. Proposed method for asynchronous multipath

 caseThe algorithm for asynchronous multipath fading is anextension of the method for the single-path synchronouscase. In this case, we collect the signals of the desired userfrom all $L$ different paths. The method of DOA estimation forthe single-path case (relation (38)) is not applicable directlysince the correlation between signals from different paths ofthe $k$-th user will hinder its applicability. We should try todecorrelate the received signal of each path from otherpaths of the $k$-th user. Without loss of generality, we assumethat the different paths of users are numbered in increasing order of path delays, i.e. $\tau_{k 1} \leq \tau_{k 2} \leq \ldots \leq \tau_{k L}$ for $k \in\{1, \ldots, K\}$. The received vector of $N_{c}$ samples of chip matched filter synchronised with $\tau_{k l}$ (the delay of the l-th path of the $k$-th user) at any antenna will contain interference of the samesymbol from the $m$ - $t h$ path of the $k$ - $t h$ user, which can berepresented by a $N_{c} \times 1$ vector as:

$$
\begin{align*}
& t_{m}=\left[t_{m}(0), \ldots, t_{m}\left(N_{c}-1\right)\right]^{T}  \tag{39}\\
& t_{m}(j)= \\
& \int_{j T_{c}+\tau_{k l}}^{(j+1) T_{c}+\tau_{k l}} s_{k}\left(t-\tau_{k m}\right) \psi^{*}\left(t-j T_{c}-\tau_{k l}\right) d t \tag{40}
\end{align*}
$$

In fact $\underline{t}_{m}$ is the interference of $m$ - $t h$ path of the $k$ th user on the l-th path of the $k$ - $t h$ one. We define the $N_{c} \times(L-1)$ matrix $C_{k l}$ with columns $\underline{t}_{m}$ for $\{m=1, \ldots, L m \neq l\}$

$$
\begin{equation*}
C_{k l}=\left[\underline{t}_{1} \vdots \underline{t}_{2} \vdots \ldots \vdots \underline{t}_{l-1} \vdots \underline{t}_{l+1} \vdots \ldots \vdots \underline{t}_{L}\right] \tag{41}
\end{equation*}
$$

The column space of matrix $C_{k l}$ (space spanned bycolumns of $C_{k l}$ ) is in fact the interference space caused bythe different paths of the $k$-th user on the $l$-th path of the $k$-thuser. To decorrelate the received signal from the $l$-th path ofthe $k$-thuser and the other paths of the $k$-th user,we just need to project the received vector of $N_{c}$ samples of the chip matched filter into a space orthogonal to the column space of matrix $C_{k l}$. The projection operator into the orthogonal space of $C_{k l}$ is [8]:

$$
\begin{equation*}
P_{k l}^{\perp}=I_{N}-C_{k l}\left(C_{k l}^{H} C_{k l}\right)^{-1} C_{k l}^{H} \tag{42}
\end{equation*}
$$

In other words, the vector $B L_{k l}^{k^{\perp}}(i)=P_{k l}^{\perp} B L_{k l}^{k}(i)$ is not affectedby other paths and is totally decorrelated fromthe usersof other path signals, then we can apply the previous method to $B L_{k l}^{k{ }^{\perp}}$ and estimate the direction of the arrival.

## IV. Simulation

In this section, the performance of the proposed method is evaluated in a multipath DS-CDMA system using gold code sequences of length 31. In all simulations, the receiver has a uniform linear array with half wavelength spacing between adjacent antennas and the antenna elements are assumed to be omnidirectional. There are eight active users $(\mathrm{K}=8)$ and three paths for each user. The real and the imaginary parts of the complex channel gains have been generated randomly by a zero mean Gaussian distribution with unit variance.

The root mean square error (RMSE) and bias versus number of data samples, SNR and number of array elements are evaluated for the first, second and third paths of 1-th user and plotted in Fig.2-7.To compare the performance of the algorithm, we compare this method with theproposed algorithms in [5], [8]and [9] in Fig. 8 and 9.In Fig. 10 and 11, the bias and RMSE of proposed algorithm for DOA estimation are illustrated for different value of SNR respectively. As we expected, with increase of SNR, bias and RMSE of proposed algorithm for DOA estimation has been decreased. In the following, to show the consistency of our algorithm the RMSE of proposed algorithm for DOA estimation is illustrated for different value of the data samples in Fig. 13. As we see in simulation result with
increase of the number of data samples RMSE tend to zero. This clearly shows the consistency of the proposed algorithm for DOA estimation.


Figure 2. RMSE versus the Number of data samples ( $\mathrm{M}=3$ )


Figure 3. Bias versus the Number of data samples ( $\mathrm{M}=3$ )


Figure 4. RMSE versus SNR ( $\mathrm{M}=3$ )


Figure 5. Bias versus $\operatorname{SNR}(\mathrm{M}=3)$


Figure 6. RMSE versus Number of Array Elements


Figure 7. Bias versus Number of Array Elements


Figure 8. Comparison of RMSE against SNR for three methods


Figure 9. Comparison of RMSE against Number of Array Elements for three methods

8 User, 3 path


Figure 10. Bias versus SNR for proposed method


Figure 11. RMSE versus SNR for propsed method


Figure 12. RMSE versus the number of data samples for proposed method

TABLE I. THE MAPPING OF SECTIONS AND BEAMFORMING FILTERS.

| section | range for <br> 2 -antenna | 2 -antenna, <br> $\mathrm{m}=$ |
| :---: | :---: | :---: |
| 1 | $-1,-3 / 4$ | 3,4 |
| 2 | $-3 / 4,-2 / 4$ | 4,3 |
| 3 | $-2 / 4,-1 / 4$ | 4,1 |
| 4 | $-1 / 4,0$ | 1,4 |
| 5 | $0,1 / 4$ | 1,2 |
| 6 | $1 / 4,2 / 4$ | 2,1 |
| 7 | $2 / 4,3 / 4$ | 2,3 |
| 8 | $3 / 4,1$ | 3,2 |

## V. Conclusion

In this paper a new method for estimating the direction of arrival of signals in frequency-selective fading channel with correlated multipaths is proposed. At first, we decorrelated the received signal of each path from other paths, and then passed it from a beam forming filter. In this approach in contrast to other DOA estimation approaches, it was not required to search all angles, and it did not require EVD. Due to the equivalency of thescenario to a DOA estimation of single source in the noise environment, AIC and MDL criteria werenot required for estimating the number of sources. Since beam forming filters wereused, the destroyingeffect ofother users on the desired users signal wasalso decreased and the efficiency of the algorithm was increasedand the search area wasdecreased almost to one tenth. Some of the other advantageous of the proposed method are, forming of correlation matrix including vectors with smaller dimension which results in lower complexity of calculation. Also, Simulations have shown that the suggested approach works properly in the case that the number of sources exceeds the number of array elements. The simulation results show that the proposed method has good stability in the multipath fading channel and the estimates of the proposed method are consistent. Intensification of the multipath fading reduces the performance of estimator. This efficiency decrease can be compensated by increasing.

## References

[1] J.G, Proakis and M.salehi 'Digital communications' $5^{\text {th }}$ edition, Mc Graw Hill press, 2008
[2] Schmidt, R.O, "Multiple Emitter Location and Signal Parameter Estimation," IEEE Trans. Antennas Propagation, Vol. AP-34, pp. 276-280, Mar. 1986.
[3] Paulraj. A, Roy, R, and Kailath, T, "Estimation of Signal Parameters via Rotational Invariance TechniquesESPRIT," Proc. 19th Asilomar Conf., Pacific Grove, CA, Nov. 1985
[4] Pillai, S. U. "Array Signal Processing," Springer Verlag, 1989
[5] C. T. Chiang and A. C. Chang, "DOA estimation in the asynchronous DS-CDMA system", IEEE Trans. Antennas and Propagation, Vol. 51, NO. 1,January 2003.
[6] Jingmin Xin; Nanning Zheng; Sano, A.; , "Subspace-Based Adaptive Method for Estimating Direction-of-Arrival With Luenberger Observer," Signal Processing, IEEE Transactions on , vol.59, no.1, pp.145-159, Jan. 2011
[7] C.C. Yao, Y. Xiaoli, K. Jay, "Space-Time Blind Delay and DOA Estimation in Chip-Asynchronous DS-CDMA systems" IEEE communication Society, Globecom 2004
[8] A. Olfat and S. Nader-Esfahani, "New receiver for multiuser detection of CDMA signals with antenna arrays", IEE Proc.Commun., Vol.151, No. 2, April 2004.
[9] M. A. Beygi and A. Olfat, "A New Subspace Method For Direction of Arrivel Estiomation of Multipath Signals in DS-CDMA Systems," in IEEE Int. Symp. On Personal, Indoor and Mobile Radio Communications (PIMRC'2007), Nov. 2007.


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